- **P5.65. a.** Sketch a power triangle for an inductive load, label the sides, and show the power angle. **b.** Repeat for a capacitive load.
- **P5.65** See Figure 5.23 in the book.
- *P5.67. Consider the circuit shown in Figure P5.67. Find the phasor current I. Find the power, reactive power, and apparent power delivered by the source. Find the power factor and state whether it is lagging or leading.

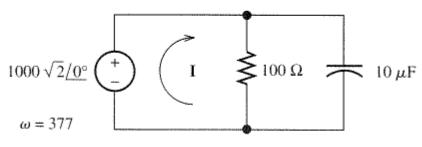


Figure P5.67

P5.67*
$$\mathbf{I} = \frac{1000\sqrt{2}\angle0^{\circ}}{100} + \frac{1000\sqrt{2}\angle0^{\circ}}{-j265.3} = 14.14 + j5.331 = 15.11\angle20.66^{\circ}$$

$$P = V_{rms}I_{rms}\cos\theta = 10 \text{ kW}$$

$$Q = V_{rms}I_{rms}\sin\theta = -3.770 \text{ kVAR}$$

$$Apparent power = V_{rms}I_{rms} = 10.68 \text{ kVA}$$

$$Power factor = \cos(20.66^{\circ}) = 0.9357 = 93.57\% \text{ leading}$$

P5.81. Find the power, reactive power, and apparent power delivered by the source in Figure P5.81. Find the power factor and state whether it is leading or lagging.

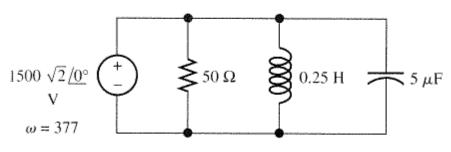


Figure P5.81

P5.81
$$P = \frac{(V_{rms})^2}{R} = \frac{1500^2}{50} = 45000 \text{ W}$$

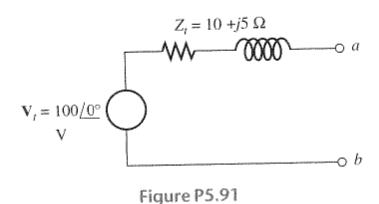
$$Q = Q_L + Q_C = \frac{(V_{rms})^2}{X_L} + \frac{(V_{rms})^2}{X_C} = \frac{1500^2}{94.25} + \frac{1500^2}{(-530.5)}$$

$$Q = 19630 \text{ VAR}$$

$$Apparent power = \sqrt{P^2 + Q^2} = 49095 \text{ VA}$$

$$Power factor = \frac{P}{Apparent power} = 91.65\% \text{ lagging}$$

*P5.91. The Thévenin equivalent of a two-terminal network is shown in Figure P5.91. The frequency is $f = 60 \,\text{Hz}$. We wish to connect a load across terminals a-b that consists of a resistance and a capacitance in parallel such that the power delivered to the resistance is maximized. Find the value of the resistance and the value of the capacitance.



P5.91* For maximum power transfer, the impedance of the load should be the complex conjugate of the Thévenin impedance:

$$Z_{load} = 10 - j5$$

 $Y_{load} = 1/Z_{load} = 0.08 + j0.04$
 $Y_{load} = 1/R_{load} + j\omega C_{load} = 0.08 + j0.04$

Setting real parts equal:

$$1/R_{load} = 0.08 \qquad R_{load} = 12.5 \,\Omega$$

Setting imaginary parts equal:

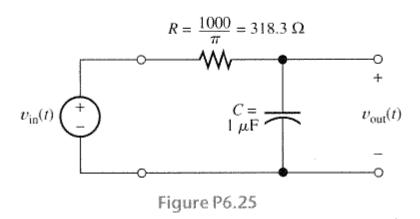
$$\omega C_{load} = 0.04$$
 $C_{load} = 106.1 \,\mu\text{F}$

- **P6.24.** In Chapter 4, we used the time constant to characterize first-order *RC* circuits. Find the relationship between the half-power frequency and the time constant.
- **P6.24** The time constant is given by $\tau = \mathcal{RC}$ and the half-power frequency is $f_{\mathcal{B}} = \frac{1}{2\pi\mathcal{RC}}$. Thus, we have $f_{\mathcal{B}} = \frac{1}{2\pi\tau}$.

*P6.25. An input signal given by

$$v_{in}(t) = 5\cos(500\pi t) + 5\cos(1000\pi t) + 5\cos(2000\pi t)$$

is applied to the lowpass RC filter shown in Figure P6.25. Find an expression for the output signal.



P6.25* The half-power frequency of the filter is

$$f_B = \frac{1}{2\pi RC} = 500 \,\mathrm{Hz}$$

The transfer function is given by Equation 6.9 in the text:

$$\mathcal{H}(f) = \frac{1}{1 + j(f/f_B)}$$

The given input signal is

$$v_m(t) = 5\cos(500\pi t) + 5\cos(1000\pi t) + 5\cos(2000\pi t)$$

which has components with frequencies of 250, 500, and 1000 Hz.

Evaluating the transfer function for these frequencies yields:

$$\mathcal{H}(250) = \frac{1}{1 + j(250/500)} = 0.8944 \angle - 26.57^{\circ}$$

$$H(500) = 0.7071 \angle -45^{\circ}$$

$$H(1000) = 0.4472 \angle -63.43^{\circ}$$

Applying the appropriate value of the transfer function to each component of the input signal yields the output:

$$v_{out}(t) = 4.472\cos(500\pi t - 26.57^{\circ}) + 3.535\cos(1000\pi t - 45^{\circ}) + 2.236\cos(2000\pi t - 63.43^{\circ})$$

- *P10.8. A diode operates in forward bias and is described by Equation 10.4, with V_T = 0.026 V. For $v_{D1} = 0.600$ V, the current is $i_{D1} = 1 \text{ mA}$. For $v_{D2} = 0.680 \text{ V}$, the current is $i_{D2} = 10$ mA. Determine the values of I_s and n.
- P10.8* The approximate form of the Shockley Equation is $i_D = I_s \exp(v_D / n V_T)$. Taking the ratio of currents for two different voltages, we have

$$\frac{i_{D1}}{i_{D2}} = \frac{\exp(v_{D1}/nV_{T})}{\exp(v_{D2}/nV_{T})} = \exp[(v_{D1}-v_{D2})/nV_{T}]$$

Solving for *n* we obtain:

$$n = \frac{v_{D1} - v_{D2}}{V_T \ln(i_{D1} / i_{D2})} = \frac{0.600 - 0.680}{0.026 \ln(1/10)} = 1.336$$

Then we have

$$I_s = \frac{i_{D1}}{\exp(v_{D1} / nV_T)} = 3.150 \times 10^{-11} \text{ A}$$

- P10.14. Suppose we have a junction diode operating at a constant temperature of 300 K. With a forward current of 1 mA, the voltage is 600 mV. Furthermore, with a current of 10 mA, the voltage is 700 mV. Find the value of n for this diode.
- P10.14 Using the approximate form of the Shockley Equation, we have

$$10^{-3} = I_s \exp(0.600/nV_T)$$
 (1)

$$10^{-2} = I_s \exp(0.700/nV_T)$$
 (2)

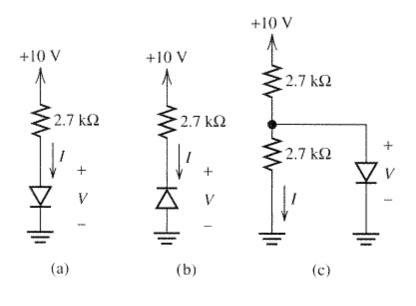
Dividing the respective sides of Equation (2) by those of Equation (1), we have

$$10 = \frac{I_s \exp(0.700/nV_T)}{I_s \exp(0.600/nV_T)} = \exp(-0.100/nV_T)$$

$$\ln(10) = 0.100/nV_T$$

$$n = 0.100/\lceil V_T \ln(10) \rceil = 1.670$$

P10.36. Find the values of *I* and *V* for the circuits of Figure P10.36, assuming that the diodes are ideal.



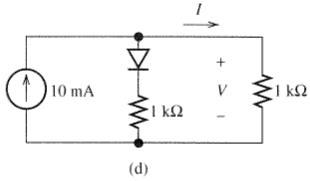


Figure P10.36

P10.36 (a) The diode is on, V = 0 and $I = \frac{10}{2700} = 3.70$ mA.

- (b) The diode is off, I = 0 and V = 10 V.
- (c) The diode is on, V = 0 and I = 0.
- (d) The diode is on, I = 5 mA and V = 5 V.